

8.2

Focus of a Parabola

For use with Activity 8.2

Essential Question Why do satellite dishes and spotlight reflectors have parabolic shapes?

1 ACTIVITY: A Property of Satellite Dishes

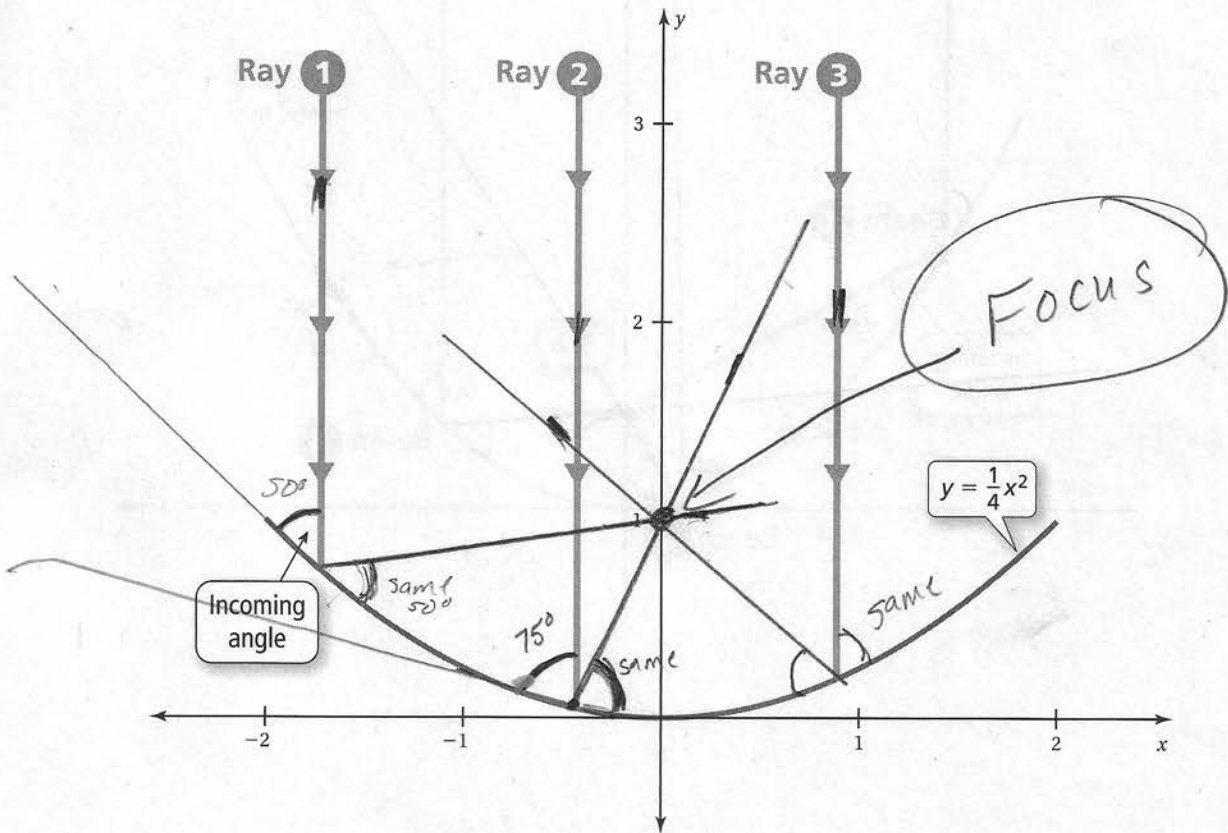
Work with a partner. Rays are coming straight down. When they hit the parabola, they reflect off at the same angle at which they entered.

- Draw the outgoing part of each ray so that it intersects the y -axis.
- What do you notice about where the reflected rays intersect the y -axis?

all go through $(0, 1)$

- Where is the receiver for the satellite dish? Explain.

$(0, 1)$ - all lines go through that point.



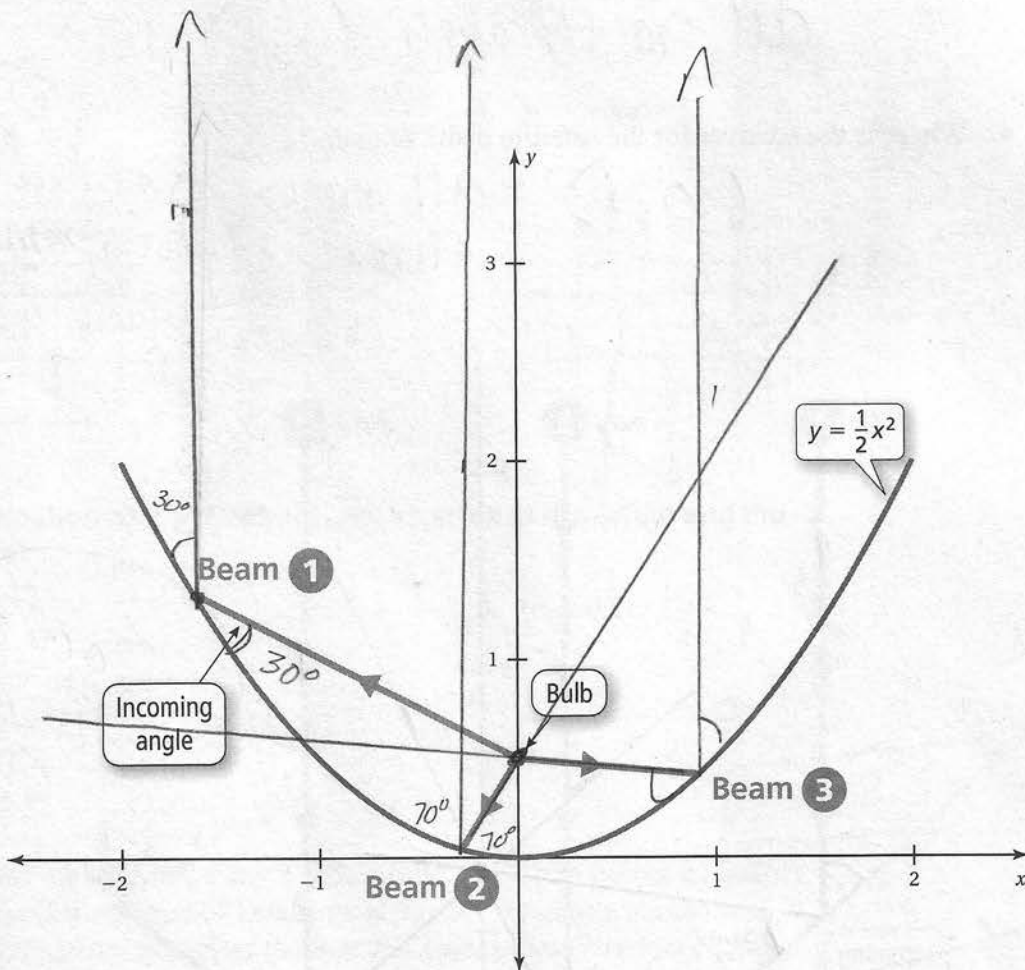
8.2 Focus of a Parabola (continued)

2 ACTIVITY: A Property of Spotlights

Work with a partner. Beams of light are coming from the bulb in a spotlight. When the beams hit the parabola, they reflect off at the same angle at which they entered.

- Draw the outgoing part of each beam. What do they have in common?
Explain.

going away → parallel to axis of symmetry



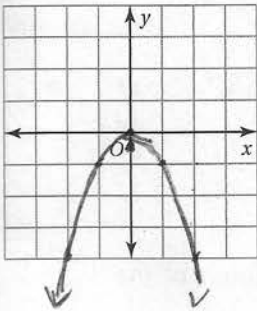
8.2

Practice

For use after Lesson 8.2

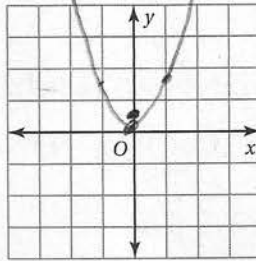
Graph the function. Identify the focus.

1. $y = -x^2$ $a = -1$



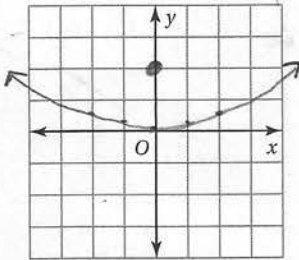
$\frac{1}{4 \cdot -1}$
 $(0, -\frac{1}{4})$
 Focus

2. $y = \frac{3}{2}x^2$



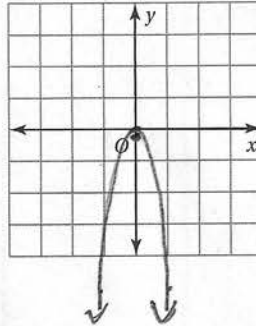
$\frac{1}{4 \cdot \frac{3}{2}}$
 $(0, \frac{1}{6})$
 Focus

3. $y = \frac{1}{8}x^2$



$\frac{1}{4 \cdot \frac{1}{8}} = \frac{1}{1/2}$
 2
 $(0, 2)$
 Focus

4. $y = -5x^2$



$\frac{1}{4 \cdot -5}$
 $-\frac{1}{20}$
 $(0, -\frac{1}{20})$
 Focus

Write an equation of the parabola with a vertex at the origin and the given focus.

5. $(0, 3)$

$\frac{1}{4a} = 3 \cdot 4a$
 $\frac{1}{4a} = 12a$

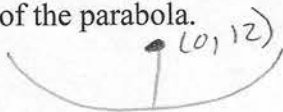
$y = \frac{1}{12}x^2$

6. $(0, -0.1)$

$\frac{1}{4a} = -.1 \cdot 4a$
 $\frac{1}{4a} = -.4a$
 $-2.5 = a$

$y = -2.5x^2$

7. A metal molding company builds a solar furnace to power its factory. The furnace consists of hundreds of mirrors forming a parabolic dish that reflects the energy of the Sun to a focal point. Write an equation for the cross section of the dish when the receiver is 12 feet from the vertex of the parabola.



$\frac{1}{4a} = 12 \cdot 4a$
 $\frac{1}{4a} = 48a$

$y = \frac{1}{48}x^2$